

# HP-67/97 program performs current-mirror analysis

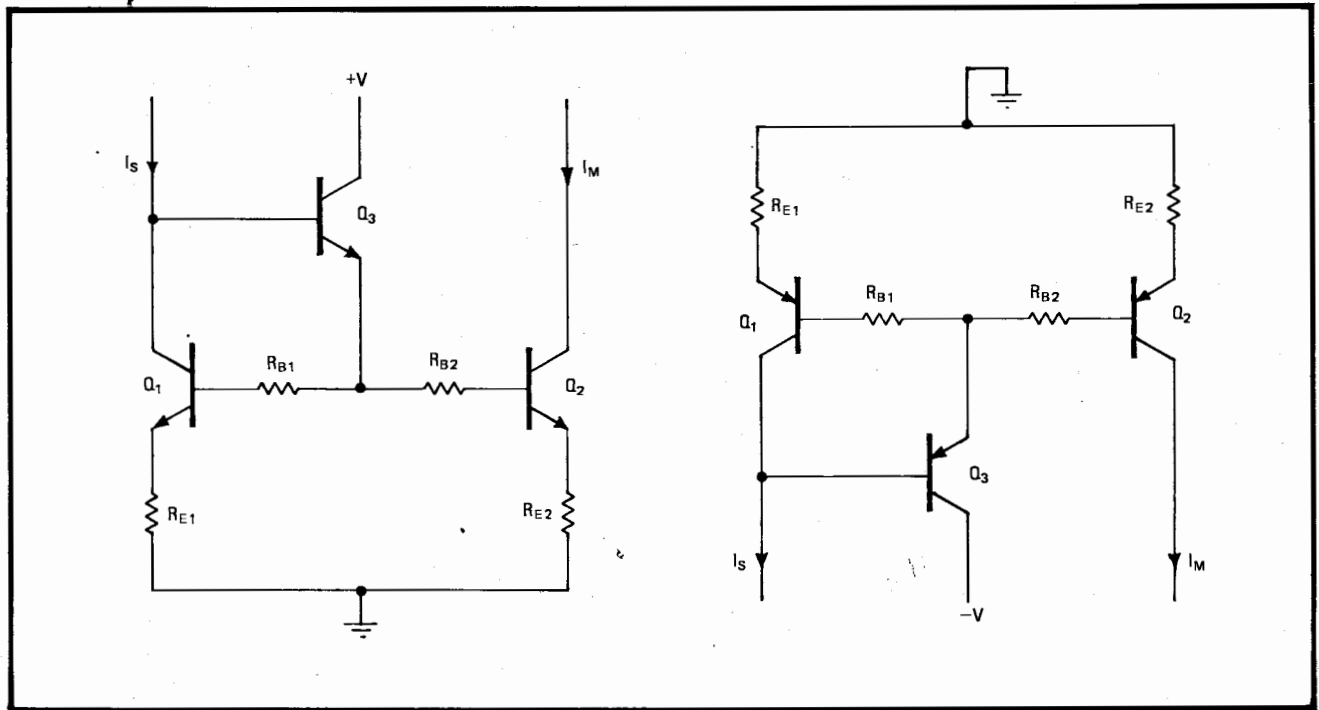
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Analysis of the dc parameters of a current mirror—that is, a slaved current generator that tracks a reference—is difficult because the equations governing the circuit are nonlinear. Using an iterative technique, however, this HP-67/97 program permits easy solution of a complex 11-variable equation and enables the mirror, which is used extensively in monolithic operational amplifiers and in numerous discrete circuits, to be designed at either a fraction of the time (if charts and nomographs are used) or cost (if a computer is used).

The program allows design of the basic mirror circuit shown in the figure, where  $I_M$ , the mirrored current, can be made either equal to or some multiple of  $I_S$ , the reference current. This arrangement may be understood if the base-to-emitter junction of transistor  $Q_3$  and resistors  $R_{B1}$ ,  $R_{B2}$ ,  $R_{E1}$ , and  $R_{E2}$  are replaced by shorts.  $Q_1$  thus acts as a diode, and because its base and emitter leads are at the same potential as the corresponding leads of  $Q_2$ ,  $I_M$  is made equal to  $I_S$ .

The loop equation describing the general circuit shown in the figure and analyzed by the program is:

$$\Delta V_{BE} + V_T \ln \frac{\beta_2(\beta_1 + 1)SI'}{(\beta_2 + 1)I_M} + I' [R_{E1}(\beta_1 + 1) + R_{B1}] - \frac{I_M}{\beta_2} [R_{E2}(\beta_2 + 1) + R_{B2}] = 0$$



**Tracking.** Program analyzes standard pnp or npn current mirror quickly and accurately. Checks of circuit sensitivity between any two circuit parameters are also performed. Setting  $\beta_3 = 0$  is permitted in order to reduce the circuit to the basic two-transistor mirror.

where:

$\Delta V_{BE}$  = the measured mismatch between  $V_{BE1}$  and  $V_{BE2}$  when  $I_{E1} = I_{E2}$

$V_T = 0.026$  volt at 298 K (25°C)

$S$  = a scaling factor given by the ratio between  $Q_2$ 's and  $Q_1$ 's emitter area

$\beta_i$  = the current gain of the  $i^{\text{th}}$  transistor.

$I'$  is given by:

$$I' = \frac{I_S(\beta_3 + 1) - I_M/\beta_2}{\beta_1(\beta_3 + 1) + 1}$$

Given any 10 parameters and an initial estimate of the remaining (unknown) quantity, the program determines the value of this last quantity by performing a Newton-Raphson iterative algorithm. In addition, it performs sensitivity analysis between any two parameters.

The program's usefulness may be seen in an example in which must be found, first, the value of  $R_{E2}$  that makes  $I_M = 25$  microamperes when  $I_S = 250 \mu\text{A}$  at  $V_{BE} = 0$ , and when  $\beta_1 = \beta_2 = \beta_3 = 100$  and  $S = 1$ ; second, the sensitivity of  $I_M$  to a 1% change in  $R_{E2}$ ; and third, the new value of  $I_M$  if  $V_{BE} = 1$  millivolt.

Keying the appropriate quantities expressed in volts, amperes, or ohms, as the case may be, into their registers (note that  $R_{E1} = R_{B1} = R_{B2} = 0$ ), and pressing f, b (see the instructions), yields  $R_{E2} = 2,371 \Omega$ . Pressing 1, ENTER, 6, f, e, reveals that there is a -69.6% change in  $I_M$  for a 1% change in  $R_{E2}$ . Pressing 1, EEX, CHS, 3, E, B, indicates that, if  $\Delta V_{BE} = 1$  mV,  $I_M = 25.29 \mu\text{A}$ .

All parameters may be altered as functions of temperature with the aid of a companion program (not shown). Additional information on both programs may be obtained either from the author or the HP-67/97 Users' Library, 1000 N. E. Circle Blvd., Corvallis, Ore. 97330. Request program library numbers 2000 and 2001. □