### Audio equalizer features transimpedance Q-enhancement topology

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In general, audio equalizers need second-order bandpass filters. Such cells require an easy and independent tuning of their parameters: the natural or central frequency, ω<sub>o</sub>; the quality factor, Q; and the maximum bandpass gain, k. The use of cells with independent adjustments could require state-variable topologies. Unfortunately, this sort of structure usually needs at least three operational amplifiers. The basis for an alternative uses SAB (single-amplifier-biquadratic) filters. These cells allow obtaining second-order bandpass filters, but they have two main drawbacks: The quality factors that you can obtain with these cells have a practical maximum limit, and you cannot independently tune the three characteristic parameters.

This Design Idea instead uses the TQE (transimpedance-Q-enhancement) structure in an audio-equalizer

(Figure 1). This cell has two advantages when you use it in equalizer circuits: You can adjust the three characteristic parameters in an independent way, but it uses only two operational amplifiers per cell. Reference 1 presents the generic TQE topology. Figure 1 shows the configuration that implements a bandpass filter based on the generic structure. This structure, which processes current-input signals, shows low-impedance input without the resistor R<sub>IN</sub>. Considering that R<sub>1</sub> and R, are equal in value and that all the capacitors are equal to C, the transimpedance, Z(s), is:

$$Z(s) = \frac{V_{BP}(s)}{I_{IN}(s)} = \frac{R_1^2 C_s}{R_1^2 C^2 s^2 + (2 - R_1 / R_2) R_1 Cs + 1}$$

However, by adding R<sub>IN</sub>, the in-

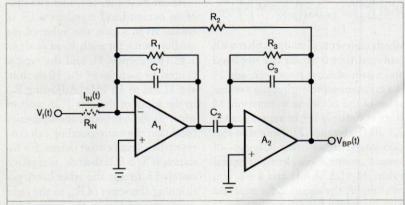


Figure 1 Adding  $R_{IN}$  to this bandpass filter based on a TQE structure causes the circuit to show high input impedance.

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put has high impedance, allowing the processing of voltage input signals because  $R_{\rm IN}$  provides the required voltage-to-current conversion. In this way, the input-to-output transfer function, H(s), is:

$$\begin{split} H(s) = & \frac{V_{BP}(s)}{V_{I}(s)} = \frac{R_{1}}{R_{IN}} \\ & \frac{s/R_{1}C}{s^{2} + s(2 - R_{1}/R_{2})/R_{1}C + 1/R_{1}^{2}C^{2}}. \end{split}$$

Thus, the circuit implements a second-order bandpass-transfer function; the following **equations** yield the central frequency,  $\omega_0$ , and the quality factor, O:

$$\omega_0 = 1/R_1C; Q = \frac{R_2}{2R_2 - R_1},$$

and the value of the gain, k, is:

$$k = \frac{R_1}{R_{IN}}Q = \frac{R_1}{R_{IN}} \left(\frac{R_2}{2R_2 - R_1}\right).$$

Thus, you can make the adjustments of  $\omega_0$ , Q, and k with  $R_1$ ,  $R_2$ , and  $R_{IN}$ , respectively.

You can use the bandpass cell in Figure 1 in an audio equalizer. Figure 2 shows a possible implementation of a

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graphic equalizer. The basis for the circuit is a bank of bandpass TQE cells. Note that the cells are TQE with lowimpedance input. Thus, the input network's  $R_{IN}$  converts  $V_{IN}(t)$  and  $V_{OUT}(t)$ to the corresponding input current, I<sub>IN</sub>(t). Adjusting potentiometer R<sub>IN</sub> with its wiper to the far left  $(X_1 \rightarrow 0)$  accentuates the frequency band that the corresponding cell covers in the overall circuit output. On the other hand, positioning the wiper of R<sub>IN</sub> to the far right  $(X_1 \rightarrow 1)$  causes a large amount of negative feedback to occur at this same frequency, thus causing attenuation in the forward-signal path. In each case, the remaining filters' TQE, receives percentages of both the input signal, V<sub>IN</sub>(t), and the output signal, V<sub>OUT</sub>(t), in ratios that their respective potentiometer settings determine.

You can derive the overall transfer function from **Figure 2**. The output voltage,  $V_{OUT}(s)$ , of the equalizer is:

$$\begin{cases} V_{OUT}(s) = -\\ V_{IN}(s) + A \sum_{l=1}^{N} Z_{I}(s) \left[ \frac{V_{IN}(s)}{X_{1}R_{IN}} + \frac{V_{OUT}(s)}{(1-X_{1})R_{IN}} \right] \right\}, \end{cases}$$

where Z<sub>1</sub>(s) are the cells' transimpedances, and

$$A = \frac{R_B}{R_A}.$$

If you define

$$H_{\rm I}(s) = Z_1(s)/R_{\rm IN},$$

then the transfer function of the equalizer becomes

$$\frac{V_{OUT}(s)}{V_{IN}(s)} = \frac{1 + A \sum_{l=1}^{N} \frac{H_{I}(s)}{X_{1}}}{1 + A \sum_{l=1}^{N} \frac{H_{I}(s)}{1 - X_{1}}}.$$

Now, you can investigate the effect of various settings of the potentiometers. For example, in the case with all of the controls centered,  $X_l$  equals 0.5 for each band. Then,  $V_{OUT}(s)/V_{IN}(s)=-1$ , as you would expect in a typical equalizer's response. Setting band I=1 to a value of  $X_l$  and all other bands flat—that is,  $X_l=0.5$  for  $I=2,3,\ldots n$ ), you obtain:

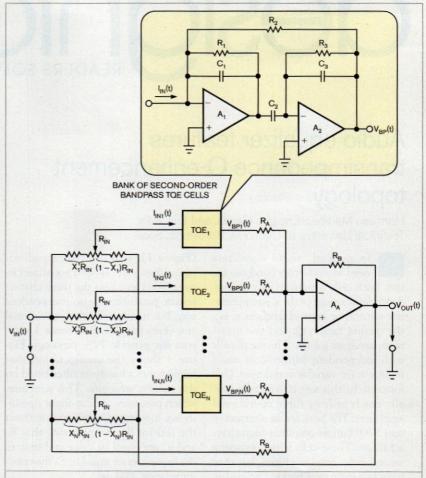


Figure 2 The TOE cells in this graphic equalizer have low-impedance inputs.

$$\begin{split} \frac{V_{OUT}(s)}{V_{IN}(s)} &= \\ s^2 + \left(\frac{\omega_{01}}{Q_1}\right) \left[1 + \frac{1}{1 + 2AM} \left(\frac{A}{X_1} - 2A\right) k\right] s + \omega_{01}^2 \\ s^2 + \left(\frac{\omega_{01}}{Q_1}\right) \left[1 + \frac{1}{1 + 2AM} \left(\frac{A}{1 - X_1} - 2A\right) k\right] s + \omega_{01}^2 \end{split}$$

which represents a bandpass filter with unity gain, or 0 dB, in the stopband and a gain of  $A_O$  at resonance, and M is a constant representing the average value of the complete summation. M is approximately 1.3, or approximately 2.3 dB (Reference 2). Note that this gain can be higher—that is, boost—or lower than one. Considering as typical values M=1.3, A=1, and k=1, you can simplify the equation for passband gain  $A_O$ , which is equal to the ratio of the s term coefficients, as:

$$A_{O} = \frac{3.6 + \left(\frac{1 - 2X_{1}}{X_{1}}\right)}{3.6 + \left[\frac{1 - 2(1 - X_{1})}{1 - X_{1}}\right]}.$$

As an example, consider the case of an octave-band equalizer with 10 bands. In this case, the value of the quality factor for each band is about 1.42 (Reference 3), and the typical central frequencies of the 10 sections are 32 Hz to 16 kHz. Adjusting R<sub>IN</sub> in the input of the cell TQE with its wiper to the left boosts the frequency band that the corresponding cell covers in the overall circuit output. For instance, if X<sub>1</sub> is 0.1, then A<sub>0</sub> is approximately 13 dB. On the other hand, positioning the wiper of R<sub>IN</sub> to the right causes attenuation in the forward-signal path. So, if X, is 0.9, then A is

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approximately -13 dB. You must have a minimum input impedance in each cell for the input voltage,  $V_{\rm IN}(t)$ , and the feedback voltage,  $V_{\rm OUT}(t)$ . Thus, the inclusion of two resistors in series with each potentiometer  $R_{\rm IN}$  in Figure 2 guarantees this resistance.EDN

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